

## HIAS MOODLE+ RESOURCE

# **HIAS Progression in Calculation**

## **Addition and Subtraction**

Hampshire Maths Team September 2023 Final version

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## **Overview**

This document gives a suggested guidance as to how calculation strategies may be taught in all year groups showing clear progression from Year 1 to Year 6.

#### Points to consider when using this resource:

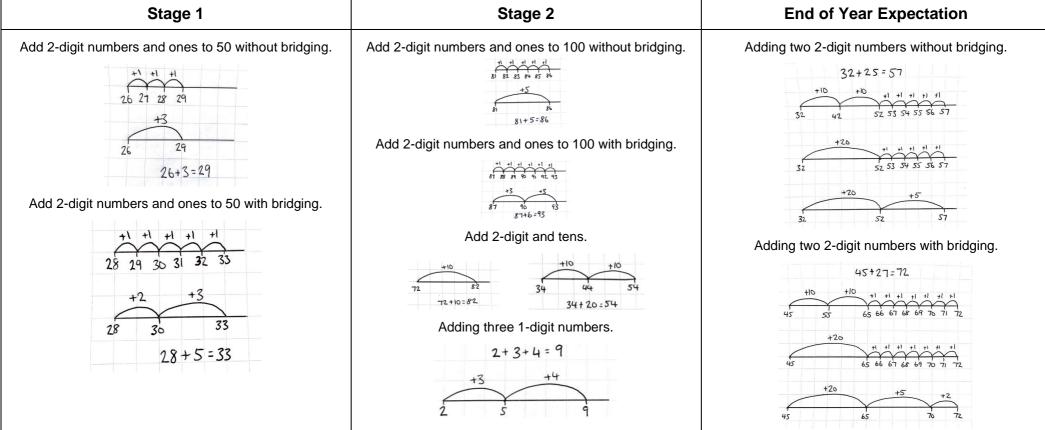
Teachers should use this resource flexibly to meet the needs of individual pupils. Teachers should be familiar with previous year groups and ensure that children are secure with concepts and strategies before moving on. Reference has been made to the National Curriculum when developing this resource and the progression within the Big Ideas provided by the NCETM. This resource works alongside Hampshire Schemes of Learning Unit plans but can also complement a blocked curriculum approach.

This document focuses upon progression in the formal calculation strategies. Manipulatives and visual representations should be used alongside the more formal recording of a strategy to ensure pupils develop both a conceptual and procedural understanding of a mathematical concept. Further details of multi-representations to support conceptual understanding/ mental fluency are detailed in the unit plans referred to within this document.

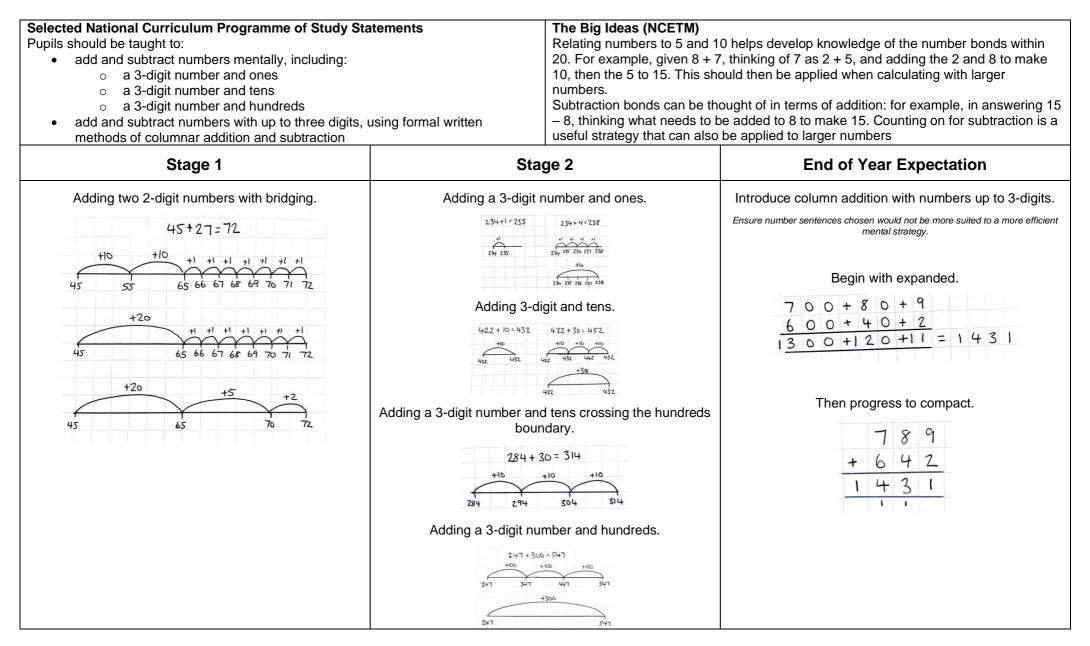
<ul> <li>Selected National Curriculum Programme of Study Statements</li> <li>Pupils should be taught to: <ul> <li>represent and use number bonds and related subtraction facts within 20.</li> <li>add and subtract 1-digit and 2-digit numbers to 20, including 0.</li> </ul> </li> </ul>		The Big Ideas (NCTEM)Relating numbers to 5 and 10 helps develop knowledge of the number bonds within20. For example, given 8 + 7, thinking of 7 as 2 + 5 and adding the 2 to 8 to make 10and then the 5 to total 15.Thinking of part whole relationships is helpful in linking addition and subtraction. Forexample, where the whole is 6, and 4 and 2 are parts. This means that 4 and 2together form the whole, which is 6 and 6 subtract 4 leaves the 2 and 6 subtract 2leaves the 4.		
Stage 1	Stage 2		End of Year Expectation	
Represent number bonds within 10. 4 + 6 = 10 $\bullet \bullet $	Use number bonds within 10. $ \begin{array}{r} +1 + 1 + 1 + 1 + 1 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \\ \hline 6 + 4 = 10 \\ \hline 6 + 4 = 10 \\ 6 + 4 = 10 \end{array} $		Represent and use number bonds within 20. $ \begin{array}{c}                                     $	
$\frac{+1}{12}$	Find 1 more from any given number within 50. 7 $30$ $33$ $31$ $34$ $40$		Add 1-digit and 2-digit numbers to 20. 12 + 4 = 16	

Linked to Hampshire Scheme of Learning Units 1.1, 1.2, 1.4, 1.5, 1.7, 1.8, 1.9 and 1.12.

Selected National Curriculum Programme of Study Statements	The Big Ideas (NCETM)
<ul> <li>Pupils should be taught to: <ul> <li>recall and use addition and subtraction facts to 20 fluently and derive and use related facts up to 100.</li> <li>add and subtract numbers using concrete objects, pictorial representations, and mentally, including: <ul> <li>a 2-digit number and ones</li> <li>a 2-digit number and tens</li> <li>two 2-digit numbers</li> <li>adding three 1-digit numbers</li> </ul> </li> </ul></li></ul>	Understanding that addition of two or more numbers can be done in any order is important to support children's fluency. When adding two numbers it can be more efficient to put the larger number first. For example, given $3 + 8$ it is easier to calculate 8 + 3. When adding three or more numbers it is helpful to look for pairs of numbers that are easy to add. For example, given $5 + 8 + 2$ it is easier to add $8 + 2$ first than to begin with $5 + 8$ . Understanding the importance of the equals sign meaning 'equivalent to' (i.e. that $6 + 4 = 10$ , $10 = 6 + 4$ and $5 + 5 = 6 + 4$ are all valid uses of the equals sign) is crucial for later work in algebra. Empty box problems can support the development of this key idea. Correct use of the equals sign should be reinforced at all times. Altering where the equals sign is placed develops fluency and flexibility.



Linked to Hampshire Scheme of Learning Units 2.1, 2.2, 2.4, 2.5, 2.7, 2.8, 2.9 and 2.12.



<ul> <li>Selected National Curriculum Programme of Study State</li> <li>Pupils should be taught to: <ul> <li>add and subtract numbers with up to 4 digits using of columnar addition and subtraction where appropriate</li> <li>solve addition and subtraction two-step problems is operations and methods to use and why</li> <li>count backwards through zero to include negative</li> </ul> </li> </ul>	g the formal written methods priate in context, deciding which	of the answer. For example be around 3000. Looking at other can help make calcula	efore carrying out a calculation to g 4786 – 2135 is close to $5000 - 20$ the numbers in a calculation and th ating easier. For example, $3012 - 2$ ich other might mean this is more e s difference.	00, so the answer will neir relationship to each 996. Noticing that
Stage 1	Stage 1 Stag		End of Year Exp	pectation
Column addition with numbers up to 3-digits. Ensure number sentences chosen would not be more suited to an efficient strategy.	Column addition with numbers up to 4-digits. Ensure number sentences chosen would not be more suited to an efficient strategy.		Multistep problem in context involving addition (Provide a mixture of opportunities to apply mental and formal strategies Some children vote for their favourite ice-cream flavour.	
789 +642 1431	39+1-5-	82	$\begin{array}{c} + & 8 & 7 & + \\ \hline 2 & 4 & 1 & 2 \\ \hline & & & \\ & & & \\ \end{array}$	4 1 3 8 7 9 auxberry = 123 Pards and Testing Agency for 2022 under Open Government Licence

Linked to Hampshire Scheme of Learning Units 4.1, 4.2, 4.7, 4.10 and 4.13.

<ul> <li>Selected National Curriculum Programme of Study Statements</li> <li>Pupils should be taught to: <ul> <li>add and subtract whole numbers with more than four digits, including using formal written methods (columnar addition and subtraction)</li> <li>solve problems involving numbers up to three decimal places.</li> <li>Interpret negative numbers in context, count forwards and backwards with positive and negative numbers through zero.</li> </ul> </li> </ul>		The Big Ideas (NCETM)Before starting any calculation is it helpful to think about whether or not you are confident that you can do it mentally. For example, 3689 + 4998 may be done mentally, but 3689 + 4756 may require paper and pencil. Carrying out an equivalent calculation might be easier than carrying out the given calculation. For example, 3682 – 2996 is equivalent to 3686 – 3000 (constant difference).	
Stage 1	Sta	ge 2	End of Year Expectation
Column addition with numbers up to 4-digits. Ensure number sentences chosen would not be more suited to an efficient strategy. 3982 +1766 5748 11 Adding involving numbers up to 1 and 2 decimal places. $3.46+1.2=4.66$ $410-46-2$	Stage 2 Column addition with numbers with more than 4-digits. Ensure number sentences chosen would not be more suited to an efficient strategy. $\begin{array}{r} 2 & 3 & 9 & 7 & 2 \\ + & 4 & 5 & 6 & 3 & 9 \\ \hline 6 & 9 & 6 & 1 & 1 \\ \hline 1 & 1 & 1 \\ \end{array}$ Adding involving numbers up to 2 decimal places. Adding with negative numbers (linking with temperature). $\begin{array}{r} -3 + 5 = 2 \\ +3 & +2 \\ \hline -3 & 0 & 2 \\ \end{array}$		Multistep problem in context, deciding which methods to use and why.         (Provide a mixture of opportunities to apply mental and formal strategies taught)         The table shares of propertunities to apply mental and formal strategies taught)         The table shares of propertunities to apply mental and formal strategies taught)         The table shares of propertunities to apply mental and formal strategies taught)         The table shares of propertunities of propertunities of a strategies taught         With the table shares of propertunities of propertunities of the strategies of th

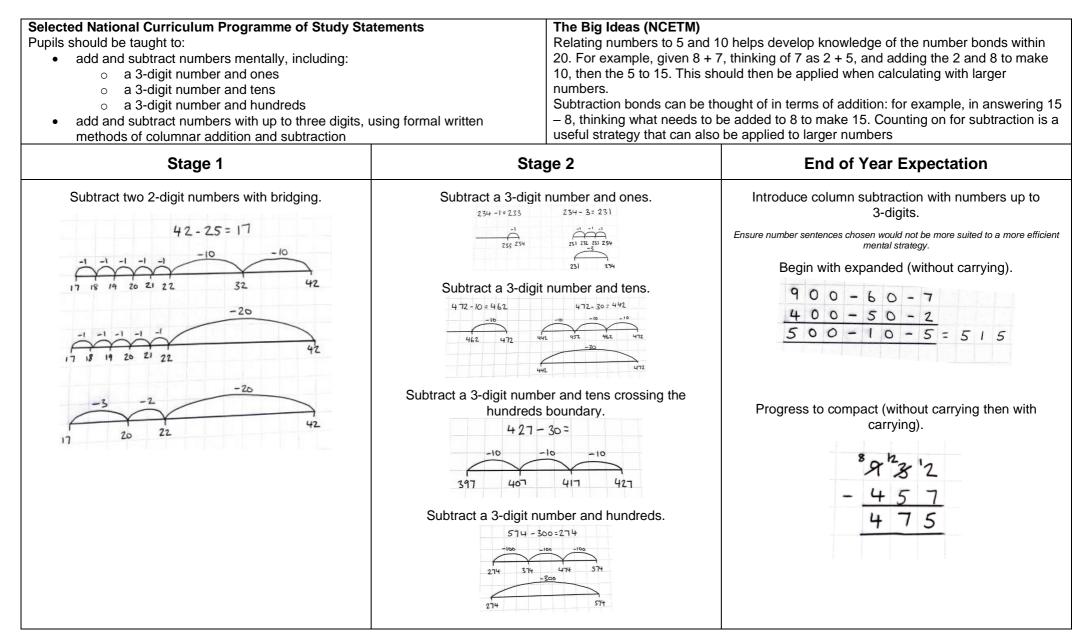
<ul> <li>Selected National Curriculum Programme of Study Sta Pupils should be taught to:</li> <li>solve addition and subtraction multi-step problems operations and methods to use and why</li> <li>use estimation to check answers to calculations and of a problem, an appropriate degree of accuracy</li> <li>use negative numbers in context, and calculate interview</li> </ul>	in contexts, deciding which nd determine, in the context	combine numbers in many v involve calculating 8.75 + 5. The associative rule helps w	nethod to use is supported by being able to take apart and vays. For example, calculating $8.78 + 5.26$ might 25 and then adjusting the answer. when adding three or more numbers: $367 + 275 + 525$ is $367 + (275 + 525)$ rather than $(367 + 275) + 525$ .
Stage 1 Stag		ge 2	End of Year Expectation
Column addition with numbers with more than 4-digits. Ensure number sentences chosen would not be more suited to an efficient strategy.	Adding negative numbers in context. Here are the temperatures in four cities at midnight and at midday.		Multistep problem in context, deciding which methods to use and why. (Provide a mixture of opportunities to apply mental and formal strategies taught)
sulled to an emclent strategy.	Temperat	ture	At the start of June, there were 1,793 toy cars in the shop.
	City At midnight	At midday	During June,
	Paris -4°C	-2°C	8,728 more toy cars were delivered
23972	Oslo -13°C	-7°C	
+ 4 5 6 3 9	Rome 3°C	10°C	9,473 toy cars were sold.
69611	Warsaw -6°C	2°C	How many toy cars were left in the shop at the end of June?
Adding involving numbers up to 3 decimal places. 3.421 + 1.234 = 4.655 +1 +0.2 +0.03 +0.655	Contains materials developed by the national curriculum assessments and li	e Standards and Testing Agency for 2018 censed under Open Government Licence (/doc/open-government-licence/version/3/	$\frac{1}{1} \begin{array}{c} 7 \\ 9 \\ 3 \\ + \\ 8 \\ 7 \\ 2 \\ 8 \\ 1 \\ 0 \\ 5 \\ 2 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1$

<ul> <li>Selected National Curriculum Programme of Study Statements</li> <li>Pupils should be taught to: <ul> <li>represent and use number bonds and related subtraction facts within 20</li> <li>add and subtract 1-digit and 2-digit numbers to 20, including 0</li> </ul> </li> </ul>		The Big Ideas (NCTEM)         Relating numbers to 5 and 10 helps develop knowledge of the number bonds within 20. For example, given 8 + 7, thinking of 7 as 2 + 5 and adding the 2 to 8 to make 10 and then the 5 to total 15         Thinking of part whole relationships is helpful in linking addition and subtraction. For example, where the whole is 6, and 4 and 2 are parts. This means that 4 and 2 together form the whole, which is 6 and 6 subtract 4 leaves the 2 and 6 subtract 2 leaves the 4.		
Stage 1	Stage 2		End of Year Expectation	
Represent number bonds within 10. $10-6 = 4$ $I_{0} = 0$	Stage 2Use number bonds within 10.		Represent and use number bonds within 20. $ \frac{4}{6} + \frac{4}{12} +$	

Linked to Hampshire Scheme of Learning Units 1.1, 1.2, 1.4, 1.5, 1.7, 1.8, 1.9 and 1.12.

<ul> <li>Selected National Curriculum Programme of Study Statements         Pupils should be taught to:         <ul> <li>recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100</li> <li>add and subtract numbers using concrete objects, pictorial representations, and mentally, including:                 <ul></ul></li></ul></li></ul>		<b>The Big Ideas (NCETM)</b> Understanding that addition of two or more numbers can be done in any order is important to support children's fluency. When adding two numbers it can be more efficient to put the larger number first. For example, given $3 + 8$ it is easier to calculate 8 + 3. When adding three or more numbers it is helpful to look for pairs of numbers that are easy to add. For example, given $5 + 8 + 2$ it is easier to add $8 + 2$ first than to begin with $5 + 8$ . Understanding the importance of the equals sign meaning 'equivaler to' (i.e. that $6 + 4 = 10$ , $10 = 6 + 4$ and $5 + 5 = 6 + 4$ are all valid uses of the equals sign) is crucial for later work in algebra. Empty box problems can support the development of this key idea. Correct use of the equals sign should be reinforced at a times. Altering where the equals sign is placed develops fluency and flexibility.		
Stage 1 Stag		ge 2	End of Year Expectation	
Subtract 2-digit numbers and ones with numbers to 50 without bridging. 26 - 3 = 23 $23 - 24$ $25 - 3 = 23$ $23 - 24$ Subtract 2-digit numbers and ones to 50 with bridging. 26 - 8 = 18 $26 - 8 = 18$ $18 - 14 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 -$	Subtract 2-digit numbers ar $85 - \frac{1}{81 \ 81}$ Subtract 2-digit numbers ar $78 \ 79 \ 80 \ 81$	s and ones to 100 without lging. 4 = 81 4 = 81 85 and ones to 100 with bridging. 7 = 78 4 = 1 = 1 85 and ones to 100 with bridging. 7 = 78 4 = 1 = 1 85 numbers and tens. 72 = 30 = 42 10 = 10 52 = 62 = 72	Subtract two 2-digit numbers without bridging. $ \frac{59 - 24 = 35}{10} + 10 + 10 + 10} $ $ \frac{59 - 24 = 35}{10} + 10 + 10 + 10} $ $ \frac{1 - 1 - 1 - 1}{10} + 10 + 10 + 10} $ $ \frac{1 - 1 - 1 - 1}{10} + 10 + 10 + 10 + 10 + 10 + 10 + 10 +$	

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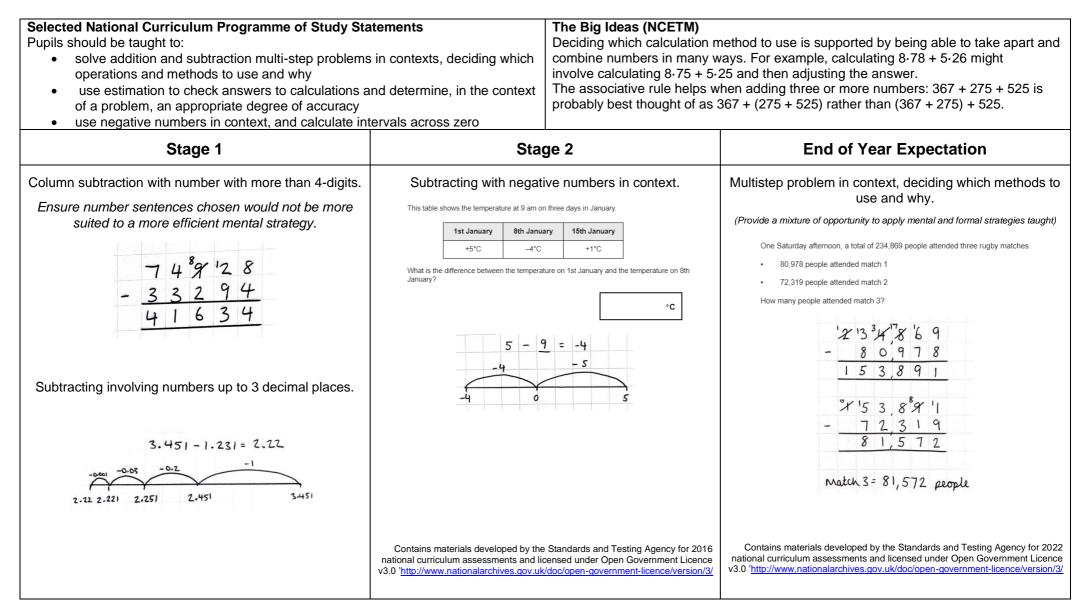


<ul> <li>Selected National Curriculum Programme of Study Statements</li> <li>Pupils should be taught to: <ul> <li>add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate</li> <li>solve addition and subtraction two-step problems in context, deciding which operations and methods to use and why</li> <li>count backwards through zero to include negative numbers (subtraction only)</li> </ul> </li> </ul>		The Big Ideas (NCETM) It helps to round numbers before carrying out a calculation to get a sense of the size of the answer. For example, 4786 – 2135 is close to 5000 – 2000, so the answer will be around 3000. Looking at the numbers in a calculation and their relationship to each other can help make calculating easier. For example, 3012 – 2996. Noticing that the numbers are close to each other might mean this is more easily calculated by thinking about subtraction as difference.	
Stage 1	Stage 1 Stage		End of Year Expectation
Column subtraction up to 3-digits. Ensure number sentences chosen would not be more suited to a more efficient mental strategy.	Column subtraction with numbers up to 4-digits. Ensure number sentences chosen would not be more suited to a more efficient mental strategy.		Two-step problem in context, deciding which methods to use and why. (Provide a mixture of opportunities to apply mental and formal strategies taught)
<sup>8</sup> 9 <sup>h</sup> 3'2 - <u>457</u> 475	$\frac{2 \cdot 8 \cdot 7 \cdot 4}{-1 \cdot 9 \cdot 4 \cdot 9}$ Count backwards through zero (linking with temperature). $\frac{5}{4}$		Ken is playing a game. He has 4,289 points. Then he scores another 355 points. Ken's target is 6,000 points. How many <b>more</b> points does Ken need to reach his target? 5673770000000000000000000000000000000000
			1711 1 × ½ 1
	-5 -4 -3 -2 -1 0 1	2 3 4 5 0	- $3 5 51 3 5 6$
		-2 -3 -4 -5	Contains materials developed by the Standards and Testing Agency for 2019 national curriculum assessments and licensed under Open Government Licence v3.0 'http://www.nationalarchives.gov.uk/doc/open-government-licence/version/3/

Linked to Hampshire Scheme of Learning Units 4.1, 4.2, 4.7, 4.10 and 4.13.

<ul> <li>Selected National Curriculum Programme of Study Statements</li> <li>Pupils should be taught to: <ul> <li>add and subtract whole numbers with more than four digits, including using formal written methods (columnar addition and subtraction)</li> <li>solve problems involving numbers up to three decimal places</li> <li>Interpret negative numbers in context, count forwards and backwards with positive and negative numbers through zero.</li> </ul> </li> </ul>		The Big Ideas (NCETM)Before starting any calculation is it helpful to think about whether or not you are confident that you can do it mentally. For example, 3689 + 4998 may be done mentally, but 3689 + 4756 may require paper and pencil. Carrying out an equivalent calculation might be easier than carrying out the given calculation. For example, 3682 – 2996 is equivalent to 3686 – 3000 (constant difference).	
Stage 1	Sta	ge 2	End of Year Expectation
Column subtraction with numbers up to 4-digits. Ensure number sentences chosen would not be more suited to a more efficient mental strategy. $\begin{array}{r} 1 & 8 & 7 & 4 \\ - & 1 & 9 & 4 & 9 \\ \hline & 1 & 9 & 2 & 5 \end{array}$ Subtracting involving numbers up to 1 and 2 decimal places. $\begin{array}{r} 3.4 & 6-1.2 = 2.2 & 6 \\ \hline & -2.2 & 2.46 & 3.46 \end{array}$	difference). Stage 2 Column subtraction with numbers up to 5-digits. Ensure number sentences chosen would not be more suited to a more efficient mental strategy. $ \begin{array}{r} 7 & 4 & 9 & 12 & 8 \\ - & 3 & 3 & 2 & 9 & 4 \\ - & 4 & 1 & 6 & 3 & 4 \\ \end{array} $ Subtracting involving numbers up to 2 decimal places. Subtracting involving numbers up to 2 decimal places. Subtract with negative numbers (linking with temperature). $ \begin{array}{r} 3.4 & 6 & -1.3 & 2 = 2.14 \\ \hline & .$		Multistep problem in context, deciding which methods to use and why.         (Provide a mixture of opportunity to apply mental and formal strategies taught)         The transmission of transmiss

Linked to Hampshire Scheme of Learning Units 5.1, 5.7, 5.10, 5.14, 5.15 and 5,18.



Linked to Hampshire Scheme of Learning Units 6.1, 6.7, 6,10 and 6.15.

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